Titration and Buffers Activity

Goal: Our goal in this activity is to introduce a straight forward strategy to predict and understand titration curves. We will be focusing on a few critical points that allow us to quickly assess most of the information that can be communicated/learned in a titration.

Definitions you should be familiar with:

$pH = -log[H_3O^+]$	$pOH = -log[OH^{-}]$	pH + pOH = 14	$[H_30^+][OH^-] = 10^{-14}$
$pK_a = -logK_a$	$pK_b = -logK_b$	$pK_a + pK_b = 14$	$pK_a * pK_b = 10^{-14}$

Let's start simple – something that you have done before:

1. Calculate the pH of a 10 mM solution of acetic acid (pKa 4.75). We will be abbreviating acetic acid as HAc and acetate Ac-. Recall that you want to start this by setting up an ICE table:

	HAc	+	H₂O (I)	1	Ac⁻	+	H₃O⁺
I							
С							
E							

2. Now do the same for a 9.09 mM solution of acetate (Ac-). Remember to use the base dissociation reaction and the Kb.

Ok, so how does this apply to titrations? Well, let's first establish what titrations are. Acid-Base Titration: The repeated addition of known amounts of a strong base into a solution containing an acid. It could also be reversed – the addition of a strong acid into a solution containing a base.

It's important to recognize the role of the STRONG acid or base here. When a strong base is added to an acid, the reaction always goes to completion – so there is not an equilibrium. Consequently, if we know how much acid and base we have, we can use the limiting reactant principle to guide us to determine the amount of reactants and products in solution.

For example:

3. If 5 mL of 100 mM NaOH is added to a 100 mL solution of 10 mM acetic acid (HAc), determine the concentration of acetate (Ac-) that is produced and the concentration of acetic acid that is left over.

Start this by writing out a reaction – note that this is a solid reaction arrow and NOT an equilibrium arrow:

NaOH (aq) + HAc
$$\rightarrow$$
 Na⁺ + Ac- + H₂O (I)

Conveniently, everything reacts with a stoichiometric coefficient of 1, so the limiting reactant is easy to find (the reactant with the smallest number of moles). Go ahead and determine the:

- a. moles of NaOH:
- b. moles of HAc:
- c. moles of products and reactants that exist after the reaction. I like to do this step as an ICE table using moles (moles because you don't need to worry about the dilution that is occurring the change will be the initial value from the limiting reactant).

	HAc	+	NaOH	\rightarrow	Ac	+	H ₂ O
Ι					0		
С							
E							

Now that you know the moles, go ahead and determine the concentration of each. Make sure to account for the extra volume that you added.

Cool, now we know the concentration of HAc and Ac-. The big question is, how did this change the pH? In problem 1, you figured out that 10 mM HAc has a pH of 3.38.

Do you expect the pH to be more acidic or basic?

Why?

Can you calculate this value? Yes, of course. You can take the concentrations you determined in problem 3, plug them into the ICE table in problem 1, do some algebra and come up with the pH. However, there is an easier way if we apply a new concept:

Buffer: A solution containing a weak acid and its conjugate base. These solutions resist change to pH when strong acids or bases are added.

You'll note that the solution that we are working with contains some weak acid (HAc) and its conjugate base (Ac-), so it is a buffer. When we are working with a buffer, we can make a safe assumptions about the chemical equilibrium (that x << initial concentrations of HAc or Ac-) and greatly simplify this calculation. Here is the math starting with the equilibrium constant Ka:

$$K_{a} = \frac{[A][H_{3}O^{+}]}{[HA]}$$
$$log K_{a} = log [H_{3}O^{+}] + log \frac{[A]}{[HA]}$$
$$-log [H_{3}O^{+}] = -log K_{a} + log \frac{[A]}{[HA]}$$
$$p H = p K_{a} + log \frac{[A]}{[HA]}$$

This new equation is the **Henderson-Hasselbalch** equation. It can be used ONLY if the **pH = pKa ± 1**.

4. Using this new equation, calculate the pH of the solution we produced in problem 3. Note that you know three of these terms.

What do you notice about the pH and pKa?

This is a special situation in titrations known as the **half-equivalence point**: when enough NaOH is added to convert exactly 50% of the weak acid to the conjugate base. In this case, the [HA] = [A-] and pH = pKa. As we'll see, this is a very useful resource when trying to understand titrations.

- 5. Try these for practice:
 - a. What is the pH when 2.5 mL of NaOH has been added?
 - b. What is the pH when 7.5 mL of NaOH has been added?

Follow exactly the same steps as above. Determine the [HAc] and [Ac-] after the NaOH is added. Then us the H-H equation

Let's define a new term now – **equivalence point:** when enough NaOH has been added to completely convert the weak acid to a weak base.

- 6. What volume of NaOH is necessary to reach the equivalence point?
 - a. How many moles of HAc are we starting with? You already figured this out in 3b.
 - b. How many moles of NaOH are needed to reach the equivalence point?
 - c. Recall that [NaOH] that you are adding is 100 mM. How many mL are necessary to reach the equivalence point?
 - d. At this point, all the HAc is now Ac-. Determine the [Ac-]. Remember to account for the volume of NaOH added.

Perhaps you noticed – the [Ac-] at this point is exactly the concentration of acetate from problem 2 – so you have already calculated the pH of this point! Let's summarize what we've calculated and label these values on the graph below. The points that are boldfaced are the 3 that you MUST know to draw a titration curve.

initial pH (calculated in problem 1) _____

pH after 2.5 mL NaOH is added (problem 5a) _____

pH after 5 mL NaOH is added (problem 4) ______

pH after 7.5 mL NaOH is added (problem 5a) _____

pH of equivalence point (problem 2 and 6) _____



Clearly label the buffer range (remember this is ±1 pH unit from the pKa).

Let's take some time to think about this more carefully in the context of the chemical makeup of the buffer. We know that the buffer is composed of HAc and Ac and we've also seen that the pH changes as this ratio changes.

- 7. Consider each of the following situations. Determine which chemical specie is in the highest concentration:
 - a. pH < pKa
 - b. pH = pKa
 - c. pH > pKa
- 8. Ok, let's put some numbers to this.
 - a. Determine the ratio of Ac-:HAc when the pH = 3.94. We know that [HAc] > [Ac-] (see previous problem), so this ratio should be less than one. Use the H-H equation and solve for the ratio.

b. If the total buffer concentration is 10 mM, calculate [HAc].

c. If the total buffer concentration is 10 mM, what is the minimum [HAc] for the solution to still be considered a buffer?